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> I. Model Problems. II. Practice III. Challenge Problems IV. Answer Key

Web Resources Rational Expressions: www.mathwarehouse.com/algebra/rational-expression/

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Addition and Subtraction of Rational Expressions-Unlike denominators

I. Model Problems

	t common multiple of rational expressions. multiple of $3x^3 + 3x^2 - 6x$ and $4x^3 - 8x + 4x$. $3x^3 + 3x^2 - 6x$ $3x(x^2 + x - 2)$ 3x(x + 2)(x - 1) 4x(x - 1)(x - 1)
List all the factors of the first expres Add any missing factors of the next expression. Simplify partially.	sion. $3x(x+2)(x-1)$ $3x(x+2)(x-1) \cdot 4(x-1)$ $12x(x+2)(x-1)^{2}$
Answer: $12x(x+2)(x-1)^2$ In this example we will add rational expressions with unlike denominators <i>Example 2:</i> Simplify and find the restrictions of $\frac{4x}{x^2+5x+6} + \frac{5}{x^2-9}$. Factor the denominators. $\frac{4x}{(x+2)(x+3)} + \frac{5}{(x+3)(x-3)}$ Find the restrictions	
Find the restrictions. The least common denominator is the leash common multiple. List all the factors of the first expression. Add any missing factors of the next expression.	$x \neq -3, -2, 3$ (x + 2)(x + 3) (x + 2)(x + 3) (x - 3)
Find equivalent expressions by multiplying the numerator of each expression by missing factor(s) in the denominator.	$\frac{4x}{(x+2)(x+3)} = \frac{4x(x-3)}{(x+2)(x+3)(x-3)}$
Add the numerators. Simplify numerators.	$\frac{5}{(x+3)(x-3)} = \frac{5(x+2)}{(x+3)(x-3)(x+2)}$ $\frac{4x^2 - 12x}{(x+2)(x+3)(x-3)} + \frac{5x+10}{(x+3)(x-3)(x+2)}$
Add numerators. Answer: $\frac{4x^2 - 7x + 10}{(x+2)(x+3)(x-3)} x \neq -3, -2$	$\frac{4x^2 - 7x + 10}{(x+2)(x+3)(x-3)}$

II. Practice Problems

Find the LCM. 1. $a^{3}b;ab^{2}$ 2. $15xy^{2};6x^{2}y^{2}$ 3. $8xy^{4};10x^{2}z^{3};4y^{5}$ 4. (x+2);(x+3)5. (x-5)(x+2);(x+5)(x-2)6. $x^{2}-4;x^{2}+4x+4$ 7. $x^{2}-2x-15;x^{2}-6x+5$ 8. $2x^{3}-14x^{2}+24x;3x^{4}-18x^{3}+27x^{2}$

Simplify and find the restrictions 9. $\frac{2}{a^3b} + \frac{3}{a^2b^4}$ 10. $\frac{3z}{x^4y} - \frac{5y}{x^3z}$ 11. $\frac{6}{4a^3b^2} + \frac{7}{10a^2b^4} - \frac{2}{5a^3b}$ 12. $\frac{5z}{16xy^2} - \frac{7x^2}{7y^3z} + \frac{3y}{12x^4z}$ 13. $\frac{3x}{x+1} + \frac{5}{x+2}$ 14. $\frac{4x}{x+3} - \frac{2}{x-5}$ 15. $\frac{3}{(x+2)(x+1)} + \frac{5}{(x+1)(x-2)} + \frac{7}{(x+2)(x-2)}$ 16. $\frac{3x}{x^2-x-6} + \frac{4}{x^2-9}$

$$\frac{1}{x^{2}+x-12} = \frac{x^{2}+9x+20}{x^{2}-10x+25} + \frac{2x}{x^{2}-x-20}$$

$$19. \frac{x-1}{(x+3)(x-4)} + \frac{3x}{(x-4)(x+2)} + \frac{2}{3x(x-4)}$$

$$20. \frac{1}{x^{2}+8x+16} + \frac{1}{x^{2}-16}$$

III. Challenge Problems

1. Find the student's error.

$$\frac{3x}{(x+3)(x-2)} - \frac{2}{(x-2)(x-3)}, x \neq -3, 2, 3$$
$$\frac{3x(x-3)}{(x+3)(x-2)(x-3)} - \frac{2(x+3)}{(x-2)(x-3)(x+3)}$$
$$\frac{3x^2 - 9x}{(x+3)(x-2)(x-3)} - \frac{2x+6}{(x-2)(x-3)(x+3)}$$

$$\frac{3x^2 - 11x + 6}{(x+3)(x-2)(x-3)}, x \neq -3, 2, 3$$

2. Find the student's error.

$$\frac{2x}{(x-5)(x+5)} + \frac{4}{(x+5)(x+5)}, x \neq -5,5$$
$$\frac{2x}{(x-5)(x+5)} + \frac{4(x-5)}{(x+5)(x-5)}$$
$$\frac{6x-20}{(x-5)(x+5)} x \neq -5,5$$

IV. Answer Key

1. a^3b^2

2.
$$30x^2y^3$$

3. $40x^2y^5z^2$
4. $(x+2)(x+3)$
5. $(x+2)(x+5)(x-5)$
6. $(x+2)^2(x-2)$
7. $(x+3)(x-5)(x-1)$
8. $6x^2(x-3)^2(x-4)$
9. $\frac{3a+2b^3}{a^3b^4}, a \neq 0; b \neq 0$
10. $\frac{3z^2-5xy^2}{x^4yz}, x \neq 0; y \neq 0; z \neq 0$
11. $\frac{30b^2+14a-8b^3}{20a^3b^4}, a \neq 0; b \neq 0$
 $\frac{15x^3yz^2-42x^6+12y^4}{48x^4y^3z}, x \neq 0; y \neq 12$
12. $0; z \neq 0$
13. $\frac{3x^2+11x+5}{20x^2}, x \neq 0, x \neq 0$

13.
$$\frac{13}{(x+1)(x+2)}, x \neq -1; x \neq -2$$

14. $\frac{4x^2 - 22x - 6}{(x+3)(x-5)}, x \neq -3; x \neq 5$
 $\frac{15x + 11}{(x+2)(x-2)(x+1)}, x \neq -2; x \neq 15$
15. $-1; x \neq 2$

$$\frac{7x^2 + 17x}{(x+2)(x-3)(x+3)}, x \neq -2; x \neq 16. -3; x \neq 3$$

 $\frac{5x^2 + 41x}{(x+4)(x-3)(x+5)}, x \neq -5; x \neq 17. -4; x \neq 3$

18.
$$\frac{7x^2 + 11x + 4}{(x+4)(x-5)^2}$$
, $x \neq 5$; $x \neq -4$

 $\frac{12x^3+32x^2+4x+12}{3x(x+2)(x+3)(x-4)}, x \neq 0; x \neq 19, -2; x \neq -3; x \neq 4$

$$20.\,\frac{2x}{(x+4)^2(x-4)}, x\neq -4,4$$

Challenge Problems

- 1. Did not distribute negative to all terms of numerator of 2nd rational expression.
- 2. Repeated factor needs to be accounted for in LCD. Correct LCD is $(x-5)(x+5)^2$

M.M. Corrections

Corrected answers are grey highlighted

2.
$$30x^2y^3$$
 $90x^2y^2$
3. $40x^2y^5z^2$ $40x^2y^5z^3$
5. $(x+2)(x+5)(x-5)$
 $(x+2)(x+5)(x-5)(x-2) = (x^2-4)(x^2-25)$
12. $\frac{15x^5yz^2-42x^6+12y^4}{48x^4y^5z}, x \neq 0; y \neq 0; z \neq 0$
 $\frac{5x^5yz^2-16x^6+4y^4}{16x^4y^5z}, x \neq 0; y \neq 0; z \neq 0$

16.
$$\frac{7x^2 + 17x}{(x+2)(x-3)(x+3)}, x \neq -2; x \neq -3; x \neq 3$$
$$\frac{3x^2 + 13x + 8}{(x+2)(x-3)(x+3)}, x \neq -2; x \neq -3; x \neq 3$$

19. $\frac{12x^3 + 32x^2 + 4x + 12}{3x(x+2)(x+3)(x-4)}, x \neq 0; x \neq -2; x \neq -3; x \neq 4$

$$\frac{12x^3 + 32x^2 + 10x + 12}{3x(x+2)(x+3)(x-4)}, x \neq 0; x \neq -2; x \neq -3; x \neq 4$$

Challenge problems are correct.